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15 June 04

Dear Atle,

It was good talking to you & Betty
last night she brings good cheer.

On August 21, 03 I sent you a
copy of your MS by air mail, and
telephoned you to say that I had done so.
I am sorry you never got it. I should
have called you again, but I was not well
enough to do so during the winter.

Here is another copy. Best regards
to you both from
both of us

Chandm

Re: the replacement copies sent by K. Chandrasekharan

1) The xerox copy that Selberg received in June 2004 had the following self-memo inscribed on the upper right corner of page 1.

KC received 29 August 95.

He [Selberg] asked for a copy on 20 Aug 2003.

Sent it on 21 Aug 2003 (air mail).

2) The copy that Chandrasekharan sent in Aug 2003 does indeed seem to be lost: it turned up neither in Selberg's office nor home.

3) Page 2 of the copy that KC received from Selberg in 1995 differed very slightly from the original transparency. See copy below.

2 (cont)

For $n \geq 1$, given a discrete lattice of translations in euclidean n space whose elements ω (each with n components $\omega^{(i)}$) are generated by n linearly independent elements ξ_1, \dots, ξ_n (with nonsingular matrix $\Omega = (\xi_j^{(i)})$). Assume the lattice is irreducible in the sense that if an element ω has one component $\omega^{(i)}$ equal to zero, then all components of ω are zero: $\omega = 0$. Denote by \mathbb{P}_∞ the group with elements $\begin{pmatrix} 1 & \omega \\ 0 & 1 \end{pmatrix}$, generated by $\begin{pmatrix} 1 & \xi_j \\ 0 & 1 \end{pmatrix}$ for $j=1, \dots, n$.

If we now adjoin to \mathbb{P}_∞ an element

$$M = \begin{pmatrix} \alpha & \beta \\ \gamma & \delta \end{pmatrix} \quad \text{with } n \text{ components } \begin{pmatrix} \alpha^{(i)} & \beta^{(i)} \\ \gamma^{(i)} & \delta^{(i)} \end{pmatrix}$$

$$\text{and } \alpha\delta - \beta\gamma = 1 \quad (\alpha^{(i)}, \beta^{(i)}, \gamma^{(i)}, \delta^{(i)} \text{ real})$$

When is the resulting group discrete?

left til later

Case $n=1$

Case $n \geq 1$

2. Put $D = \|\xi_j^{(i)}\| = \|\Omega\|$.

From a theorem of Minkowski:

For $t_i > 0$ and $\prod_{i=1}^n t_i \geq D \exists \omega \neq 0$

with $|\omega^{(i)}| \leq t_i$ for $i=1, \dots, n$.

will be used repeatedly.