

□

$$W_{k,h}(z, \xi) = \sum \Sigma_{\gamma}^{-k}(z) w_{k,h}(\gamma z, \xi)$$

$$= \sum \frac{1}{\Sigma_{\gamma^{-1}}(\xi)}^{-h} w_{k,h}(z, \gamma^{-1}\xi)$$

$$\Sigma_{\gamma_1}^{-k} w_{k,h}(\gamma_1 z, \xi) = \sum \Sigma_{\gamma}^{-k}(\gamma_1 z) \sqrt{\Sigma_{\gamma_1}^{-k}(z)} w_{k,h}(\gamma \gamma_1 z, \xi)$$

$$= \sum \Sigma_{\gamma \gamma_1}^{-k}(z) w_{k,h}(\gamma \gamma_1 z, \xi) = W_{k,h}(z, \xi)$$

$$W_{k,h}(\gamma z, \xi) = \Sigma_{\gamma}^k(z) W_{k,h}(z, \xi).$$

$$W_{k,h}(z, \gamma_1 \xi) = \frac{1}{\Sigma_{\gamma_1}(\xi)} w_{k,h}(z, \xi)$$

$$W_{k,h}(\gamma_1 z, \gamma_2 \xi) = \Sigma_{\gamma_1}^k(z) \frac{1}{\Sigma_{\gamma_2}(\xi)}^{-h} W_{k,h}(z, \xi)$$

$$w_{k,h}(\gamma z, \gamma \xi) = \Sigma_{\gamma}^k(z) \frac{1}{\Sigma_{\gamma}(\xi)}^{-h} w_{k,h}(z, \xi).$$

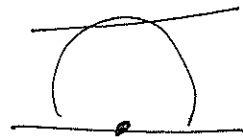
$$w_{k,h}(z, \xi) = \left( \frac{z-\xi}{z-\bar{\xi}} \right)^{h-k} \left( \frac{\xi-\bar{z}}{\xi-\xi} \right)^k ; h \geq k$$

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$$\iint k(z, \xi) \eta^s y^s d\omega_\xi d\omega_z$$

$$\iint k(z, \xi) \frac{\eta^{s'} y^s}{|z|^{2s}} d\omega_\xi d\omega_z$$

$$\iint h(r) \frac{y^{s'+s-2}}{|z|^{2s}} d\omega_z dx dy$$



$$x = y \cdot t$$

$$\iint \frac{y^\alpha}{(x^2 + y^2)^s} dx dy$$

$$\frac{dx = y dt}{}$$

cannot be done

$$\int_0^\infty \frac{y^{\alpha+1}}{y^{2s}} dy$$

$$\iint_S \sum W_{k,h}(z, \xi) \overline{W_{k,h}(z', \xi^*)} d\omega_\xi$$

$$W_{k,h}(z, \xi) \sum \overline{\varepsilon_\gamma^{-h}(\xi)} W_{k,h}(z', \gamma\xi) d\omega_\xi$$

$$W_{k,h}(z, \gamma\xi) \overline{w_{k,h}(z', \gamma\xi)} d\omega_\xi$$

$$\iint_S W_{k,h}(z, \xi) \overline{w_{k,h}(z', \xi)} d\omega_\xi$$

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$$W_{k,k}^*(z, z')$$

$$= \sum \varepsilon_{\gamma}^{-k}(z) w_{k,k}^*(\gamma z, z')$$

$$w_{k,k}^*(z, z') = \iint_S w_{k,h}(z, \xi) \overline{w_{k,h}(z', \xi)} d\omega_{\xi}$$

$$H_1(\Omega) \text{ of } S \quad H_1(\Omega) \\ H_k(\Omega) \quad \overline{H_h(\Omega)}$$

$$w_{k,h}(z, \xi) = \sum H(n) u_n^k(z) \overline{u_n^h(\xi)}$$

$$W_{k,k}^*(z, z') = \sum |H(n)|^2 u_n^k(z) u_n^k(z')$$

$$|H(n)| \quad \varepsilon_{h,k}$$

$$H(n) =$$

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kernel

$$\frac{y^\delta \eta^\delta}{|z - \bar{\xi}|^{2s}} \left( \frac{z - \xi}{z - \bar{\xi}} \right)^h \left( \frac{\xi - \bar{z}}{z - \bar{\xi}} \right)^\alpha$$

$$y^{\delta'}$$

$\alpha \rightarrow k \quad h \rightarrow h-k$

$h-k-v-1$

$s' = \frac{1}{2} + i\nu$

$$\frac{4\pi}{2^{2s}} \frac{\Gamma(2s-1)}{\Gamma(2s+h-1)} \sum_{v=0}^h (-1)^v \binom{h}{v} \frac{\Gamma(s+s'+v-1) \Gamma(s-s'+h-v-1)}{\Gamma(s+\alpha+v) \Gamma(s-\alpha-v)}$$

$$\frac{4\pi}{2^{2s}} \frac{\Gamma(2s-1)}{\Gamma(2s+h-k-1)} \sum_{v=0}^{h-k} (-1)^v \binom{h-k}{v} \frac{\Gamma(s-\frac{1}{2}+i\nu+v) \Gamma(s-\frac{1}{2}-i\nu+h-k-v)}{\Gamma(s+k+v) \Gamma(s-k-v)}$$

$$\frac{\Gamma(s-\frac{1}{2}+i\nu) \Gamma(s-\frac{1}{2}-i\nu+h-k)}{\Gamma(s+h) \Gamma(s-k)} + (-1)^{h-k} \frac{\Gamma(s-\frac{1}{2}+i\nu+h-k) \Gamma(s-\frac{1}{2}-i\nu)}{\Gamma(s+h) \Gamma(s-k)}$$

$$\Gamma(s-\frac{1}{2}+i\nu) \left\{ \frac{\Gamma(s-\frac{1}{2}-i\nu+h-k)}{\Gamma(s+h) \Gamma(s-k)} + (-1)^{h-k} \frac{\Gamma(s-\frac{1}{2}-i\nu+h-k) \Gamma(s-\frac{1}{2}-i\nu)}{\Gamma(s+h) \Gamma(s-k)} \right\}$$

$$1 - \left| \frac{z-\xi}{z-\bar{\xi}} \right|^2 = \frac{4y\eta}{|z-\bar{\xi}|^2} \quad s=1$$

$(s-1+v)(s+h-k-v)$

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$h > k; \quad \Delta = h - k$

$$\left( T - \frac{|z - \bar{\xi}|^2}{4\eta} \right) \left( \frac{z - \xi}{z - \bar{\xi}} \right)^\Delta \left( \frac{\xi - \bar{z}}{z - \bar{\xi}} \right)^k$$

$$\iint \left( T - \frac{(1+\eta)^2 + \xi^2}{\eta} \right) \left( \frac{1-\eta + i\xi}{1+\eta + i\xi} \right)^\Delta \left( \frac{1+\eta - i\xi}{1+\eta + i\xi} \right)^k \eta^\Delta d\xi d\eta$$

$$w = -\frac{\xi - i}{\xi + i} = \frac{1 + i\xi}{1 - i\xi} \quad \left| \frac{1 + i\xi}{1 - i\xi} \right|$$

$$1 - |w|^2 = 1 - \frac{(1 + i\xi)(1 - i\bar{\xi})}{(1 - i\xi)(1 + i\bar{\xi})} = \frac{1 + i\xi}{1 - i\xi}$$

$$= 1 - i\xi + i\bar{\xi} + |\xi|^2 - 1 + i\xi - i\bar{\xi} - |\xi|^2$$

$$-2i(\xi - \bar{\xi}) = \frac{4\eta}{(1+\eta)^2 + \xi^2} \left( \frac{1+w}{1+\bar{w}} \right)^k$$

$$\left( T - \frac{\eta}{1 - |w|^2} \right) w^\Delta \left( \frac{1 - |w|^2}{|1 + \bar{w}|^2} \right)^\Delta \sqrt{\frac{dw d\bar{w}}{(1 - |w|^2)^2}}$$

$$\eta = \frac{\frac{1-w}{1+w} + \frac{1-\bar{w}}{1+\bar{w}}}{2}$$

$$w - i\xi w = 1 + i\xi$$

$$i\xi(1+w) = w - 1$$

$$\xi = i \frac{1-w}{1+w}$$

$$\eta = \frac{1 - |w|^2}{|1+w|^2} \int \frac{ds}{1 - s^2}$$

$$1 + \bar{w} - w - |w|^2 \quad 1 + w - \bar{w} - |w|^2$$

$$\frac{1 + \frac{1-\bar{w}}{1+\bar{w}}}{1 + \frac{1-w}{1+w}} = \frac{\frac{2}{1+\bar{w}}}{\frac{2}{1+w}} = \frac{1+w}{1+\bar{w}}$$

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$$\iint \left( T - \frac{y}{1-|w|^2} \right) w^\Delta \left( \frac{1-|w|^2}{|1+w|^2} \right)^\Delta \left( \frac{1+w}{1+\bar{w}} \right)^k \frac{du dv}{(1-|w|^2)^2}$$

$\frac{d\mathcal{E}}{d\mathcal{V}}$

$$\iint \left( T - \frac{y}{1-|w|^2} \right) \frac{(1-|w|^2)^{\Delta-2} w^\Delta}{(1+w)^{\Delta-k} (1+\bar{w})^{\Delta+k}} du dv$$

$$\left( T - \frac{y}{1-r^2} \right) \frac{(1-r^2)^{\Delta-2} r^{\Delta+1} e^{i\Delta\varphi}}{(1+re^{i\varphi})^{\Delta-k} (1+r\bar{e}^{i\varphi})^{\Delta+k}} dr d\varphi$$

$$\sum \binom{-\Delta+k}{\nu} \binom{-\Delta-k}{\nu+\Delta} r^{2\nu}$$

$$1-r^2 = \frac{y}{T}$$

$$r^2 = 1 - \frac{y}{T}$$

$(-1)^\Delta$

$$\frac{(-\Delta+k) \dots (-\Delta+k-\nu+1) (-\Delta-k) \dots (-\Delta-k-\nu+1)}{\nu!^2}$$

$$\frac{(\Delta+h+\nu-1) \dots (\Delta-k) \cdot (\Delta+\nu-k-1) \dots (\Delta-k)}{\nu! (\nu+\Delta)!}$$

$$\sum_{\nu} \binom{\Delta+h+\nu-1}{\nu+\Delta} \binom{\Delta+\nu-k-1}{\nu} r^{2\nu+2\Delta+1}$$