

let $U(s)$ harmonic eq. zero on boundary D
 ρ run over zeros inside.

then

$$\sum_{\rho} U(\rho) = -\frac{1}{24} \int_D \log |f(\sigma)| \frac{\partial U}{\partial n} |d\sigma|$$

take

$$U(s) = \frac{4T}{\pi} \cos \frac{\pi}{4T} t \cdot \sinh \frac{\pi}{4T} (\sigma - \alpha)$$

$$\rho = \beta + iy$$

$$\sum_{|y| < T} \beta - \alpha < c \int_{-2T}^{2T} \log |f(\alpha + it)| dt$$

$$+ c \int_{\alpha}^{\infty} \log |f(\sigma + 2iT)| \sinh \frac{\pi}{4T} (\sigma - \alpha) d\sigma$$

1. Form of large sieve with pseudo characters:
2. Form of combination with integral inequality.
3. Auxiliary functions, & estimations
4. Littlewood's Lemma, & techniques for estimation of integrals $\int \log(1+u+w)$
5. Choice of parameters & final result.
6. Endremarks, about the method.

$$a_n = \sum_{d|m} \lambda_d$$

$$\lambda_d = \mu(d) \text{ for } d \leq z$$

$$\lambda_d = \mu(d) \frac{\log \frac{z}{d}}{\log z} \text{ for } z < d \leq zf$$

z square free.

$$z \leq d < zf$$

$$\psi_q(n) \text{ multiplicative } \psi_q(n) = \prod_{p|n} \psi_q(p)$$

for $\sigma > 1$. have χ ^{primitive} char mod $q_1, (q_1, q_2) = 1$
 q_2 square free

$$\sum_n \frac{\chi(n) \psi_{q_2}(n) a_n}{n^s}$$

$$= L(s, \chi) M(s, \chi, \psi)$$

with

$$M(s, \chi, \psi) = \sum_d \lambda_d \chi(d) \psi_{q_2}(d)$$

$$= \sum_d \frac{\lambda_d \chi(d) \psi_{q_2}(d)}{d^s} \prod_{\substack{p|q_2 \\ (d, p) < q_2}} (1 - \chi(p) p^{1-s})$$

$$\frac{1}{2}(\delta_1^2 + \delta_2^2) = \frac{1}{2} \frac{1}{s^2} + \frac{1}{2} \frac{1}{(s+1)^2} \delta_1 + \delta_2$$

$$\sum_{d|n} \frac{\lambda d}{d^2} \quad \sum_{d|1} \frac{s+\frac{3}{2}}{(s+1)^2} < \frac{1}{s+\frac{1}{2}}$$

$$TQ^2 \sum z^{1-2\sigma}$$

$$Z = TQ^2$$

$$x = (\sqrt{TQ} ZY)^{HE}$$

That is the one.

$$\frac{1}{p} \int \left(\frac{z}{p}\right)^s \frac{\prod (1-p^{-1-s})}{p/p} ds$$

$$M \sum \frac{z^s}{d^{2s}} \frac{1}{p^{s-1}} \quad M \sum \left(\sum_{d|p} \frac{\lambda d}{d^2} \right)^2 +$$

$$\frac{1}{p} \prod (1-p^{-1}) + O\left(\frac{1}{p^{1-2\sigma}}\right)$$

$$A \cdot e^{-\frac{1}{2} \frac{a}{\sqrt{p}} t} \left| \frac{A}{B} - \frac{A'}{B'} \right| \frac{1}{\sqrt{p}} \left(\frac{z}{p}\right)^{-\sigma} \prod (1-p^{-1-s}) \sum |a_n|^{1-2\sigma}$$

$$e^{-\frac{1}{2} \frac{a}{\sqrt{p}} t} + \frac{1}{\sqrt{p}} \frac{1}{B} e^{-\frac{1}{2} \frac{a}{\sqrt{p}} t} - \frac{1}{2} \frac{a}{\sqrt{p}} t - \frac{1}{2} \frac{a}{\sqrt{p}} t$$

$$\frac{2t}{t^2} e^{-\frac{a}{2t}} dt \quad e^{-c\sqrt{a}}$$

$$\sum_{d \leq z} \frac{\mu(d)}{d} \frac{1}{d} = \frac{1}{p} \prod (1-p^{-1})$$

$$h p < z \quad O\left(\frac{\prod (1+p^{-\frac{3}{2}})}{p^{1+\frac{3}{2}}}\right) + O\left(\frac{\prod (1+p^{-\frac{3}{2}})}{p^{1+\frac{3}{2}}}\right)$$